

## Supporting information

# Estimation of pigment concentration in LDPE *via* in-line hyperspectral imaging and machine learning

Georgiana Amariei<sup>†</sup>, Anne Sofie Schaarup-Kjær<sup>†,‡</sup>, Pernille Klarskov<sup>£</sup>, Martin Lahn Henriksen<sup>†</sup>, Mogens Hinge<sup>†\*</sup>

<sup>†</sup>Plastic and Polymer Engineering, Department of Biological and Chemical Engineering, Aarhus University, Aabogade 40, DK-8200 Aarhus N., Denmark.

<sup>‡</sup>American AVK Company, Quality Department, 2155 Meridian Blvd, Minden, NV 89423, USA.

<sup>£</sup>Terahertz Photonics, Department of Electrical and Computer Engineering, Aarhus University, Finlandsgade 22, DK-8200, Aarhus N, Denmark

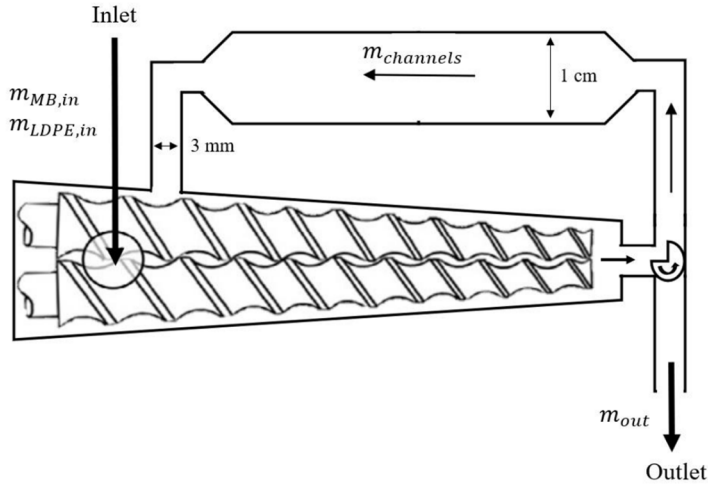
\* Corresponding authors: [hinge@bce.au.dk](mailto:hinge@bce.au.dk)

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## S1. Samples preparation

Schematic of the twin-screw extruder for compounding of the samples. The inlet and outlet are marked.



### Concentration calculation

*Assumptions:* The concentration in the channels was always equal to the concentration out ( $x_{out}$ ) of the extruder, and the pigment concentration of the pure LDPE was zero. The calculation of the concentration assumes homogenic mixing and no effect from dead zones in the compounder both in the feeding zone, screw zone, channels, and recycling chamber.

*Mass balance equations:*

Initial run:

$$m_{total,in} = m_{MB,in} + m_{LDPE,in} \quad (S1)$$

$$m_{channels} = m_{total,in} - m_{out} \quad (S2)$$

$$x_{out_{n=1 \text{ and } 2}} = \frac{m_{MB,in} \cdot x_{MB} + m_{LDPE,in} \cdot x_{LDPE}}{m_{total,in}} \quad (S3)$$

When new LDPE is added:

$$x_{channels} = x_{out_{n-1}} \quad (S4)$$

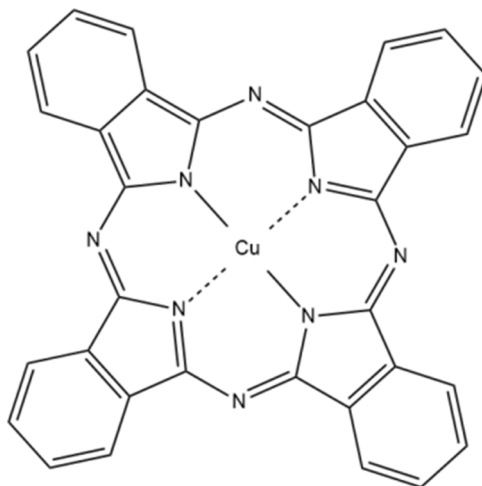
$$m_{channels} = m_{channels_{n-1}} + m_{LDPE,in} - m_{out} \quad (S5)$$

$$x_{out} = \frac{m_{channels} \cdot x_{channels} + m_{LDPE,in} \cdot x_{LDPE}}{m_{LDPE,in} + m_{channels}} \quad (S6)$$

Where,  $x$ : pigment concentration in wt%,  $m_{in}$ : mass going into the extruder of either MB, LDPE or total,  $m_{channels}$ : total mass in channels and recycling chamber,  $n$ : the cycle number.

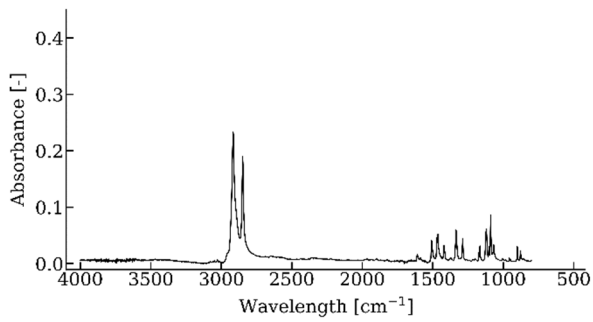
### Pigment Blue 15:3

Molecular structure of Pigment Blue 15:3 (Copper (II) phthalocyanine,  $C_{32}H_{16}CuN_8$ , CAS 147-14-8) pigment.

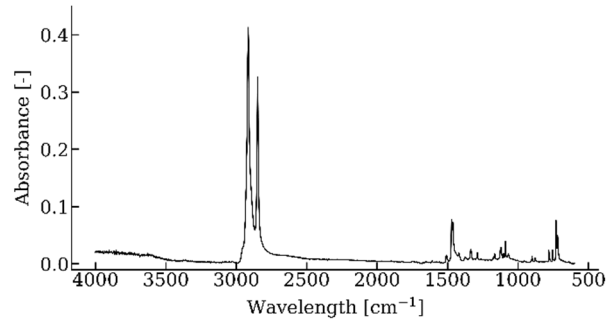


## S2. ATR FTIR spectra of all materials

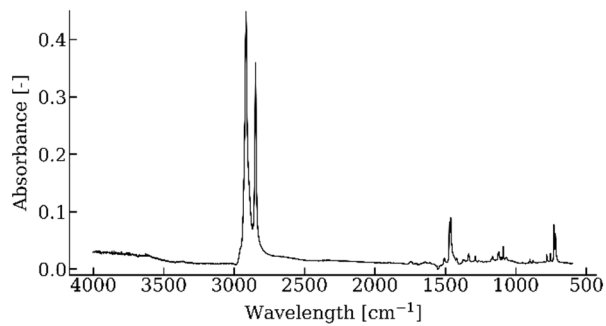
MB 40 wt%



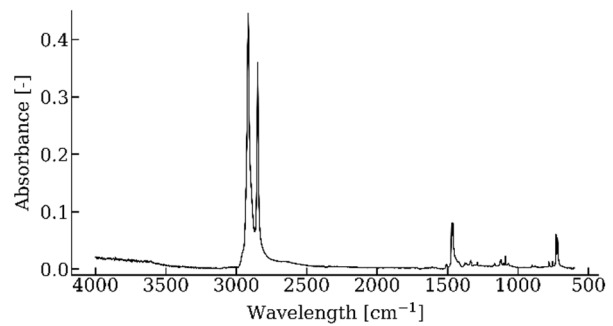
10 wt%



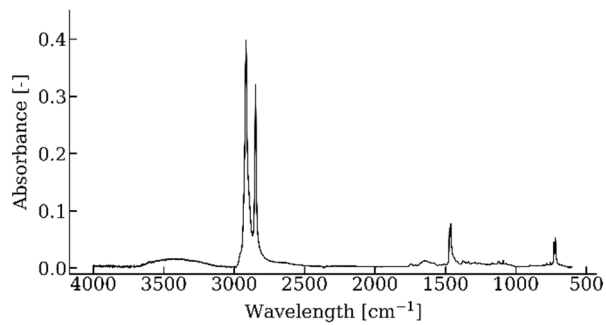
4.5 wt%



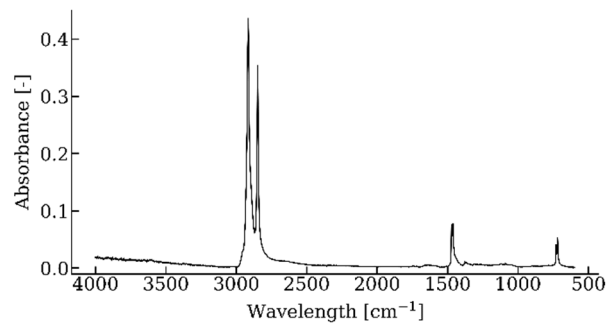
2.0 wt%



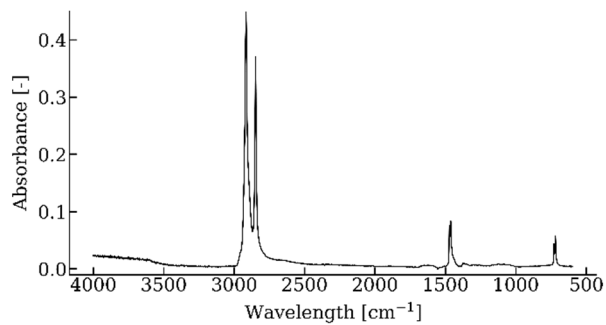
0.83 wt%



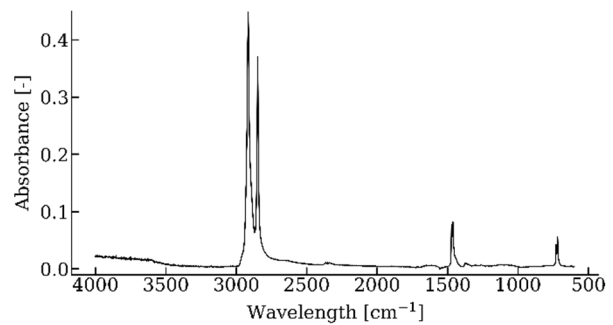
0.35 wt%



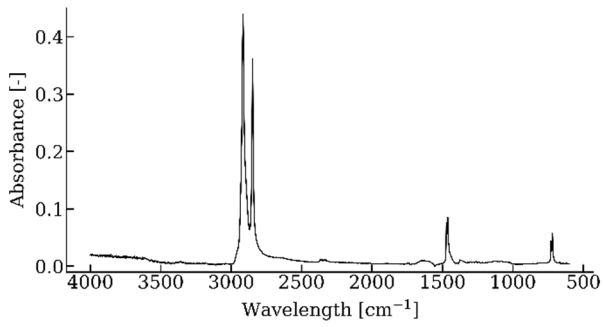
0.15 wt%



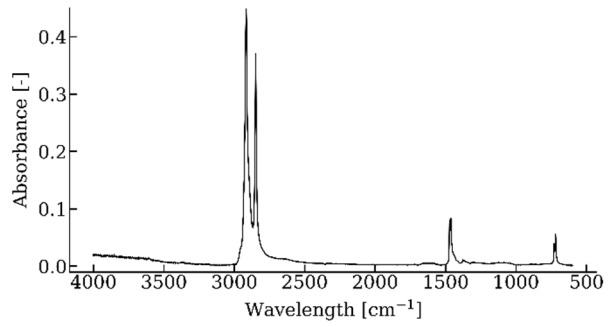
60·10<sup>-3</sup> wt%



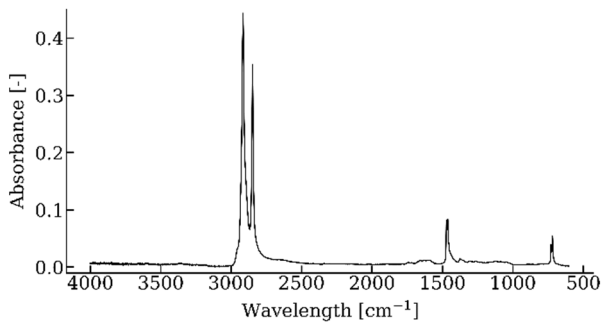
$24 \cdot 10^{-3}$  wt%



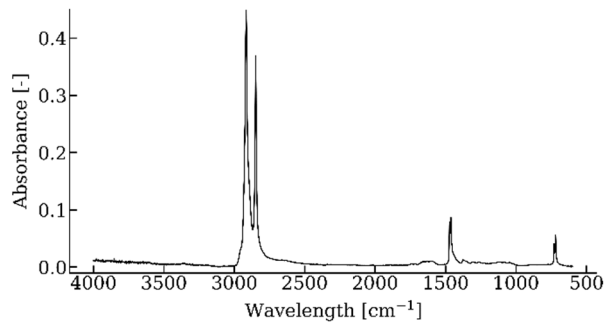
$10 \cdot 10^{-3}$  wt%



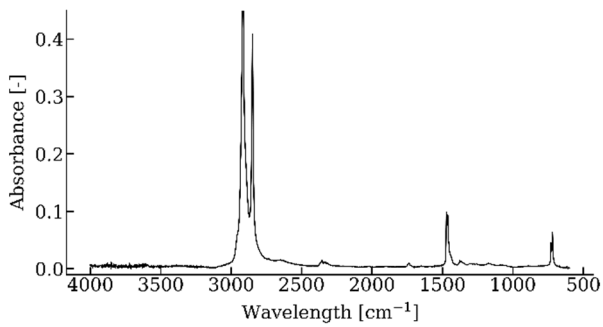
$4.0 \cdot 10^{-3}$  wt%



$1.7 \cdot 10^{-3}$  wt%

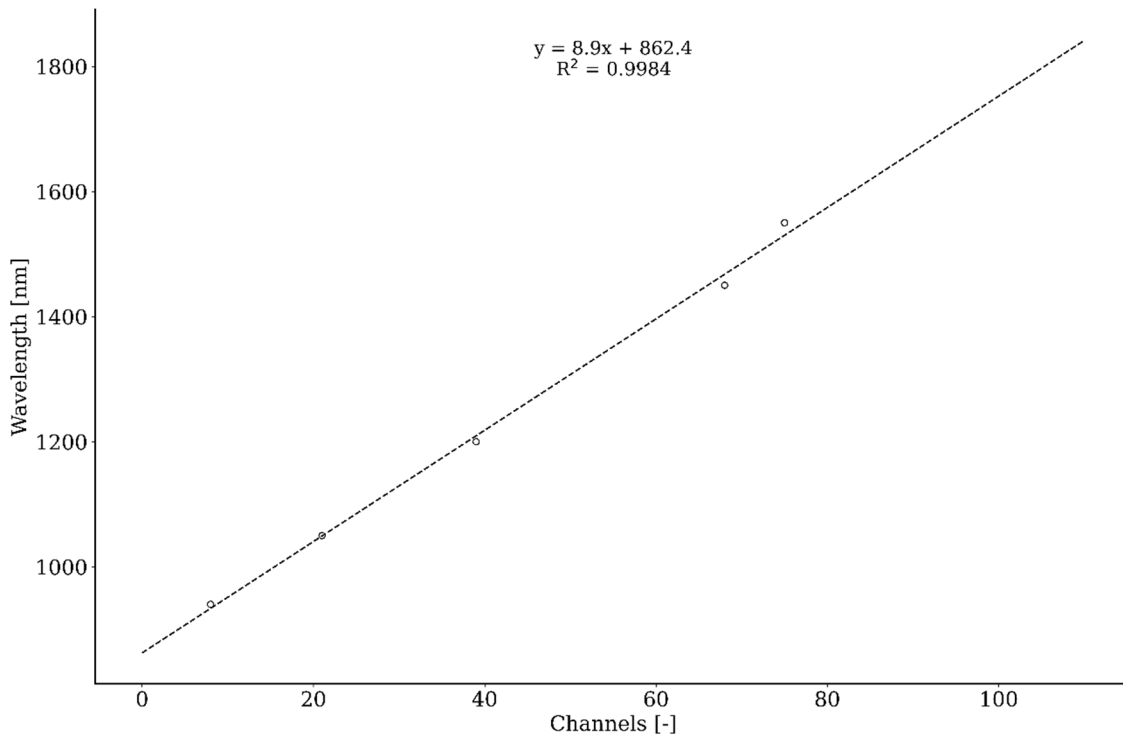
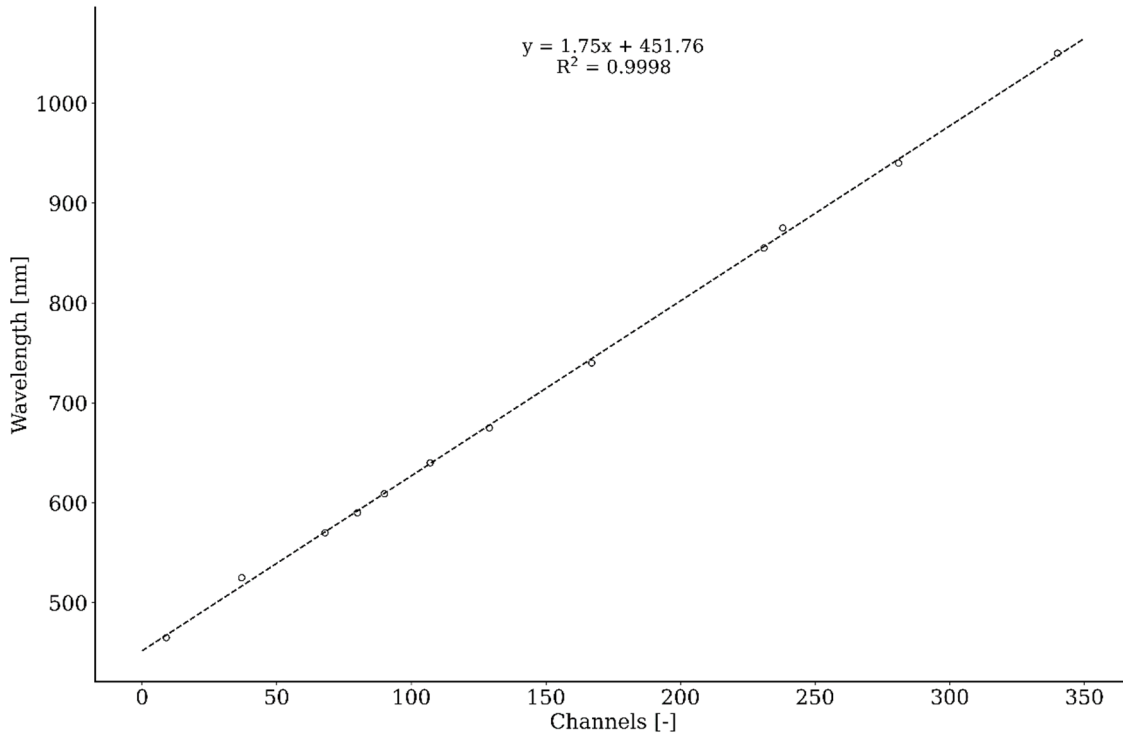


0 wt%



### S3. Hyperspectral camera calibration

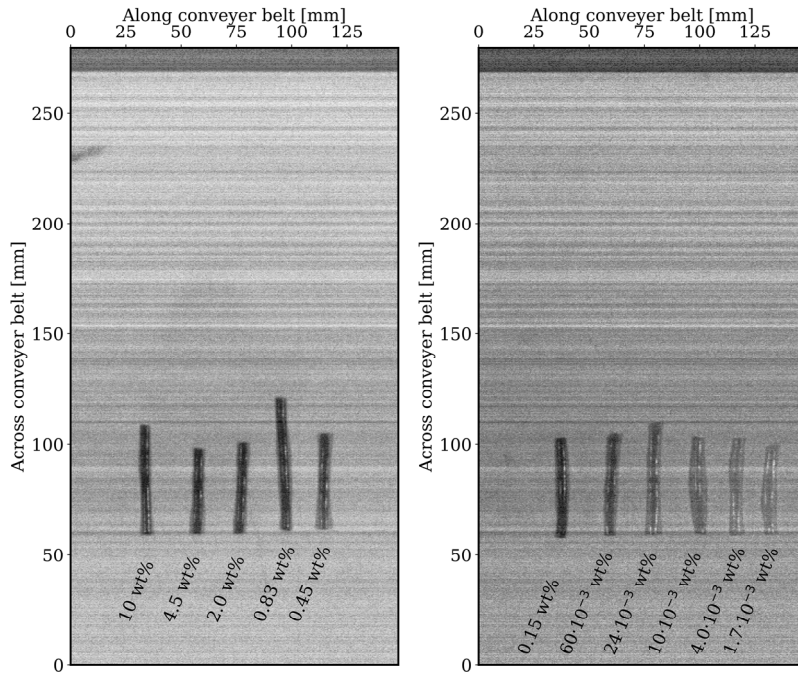
Spectral calibration of Vis/NIR and SWIR regions



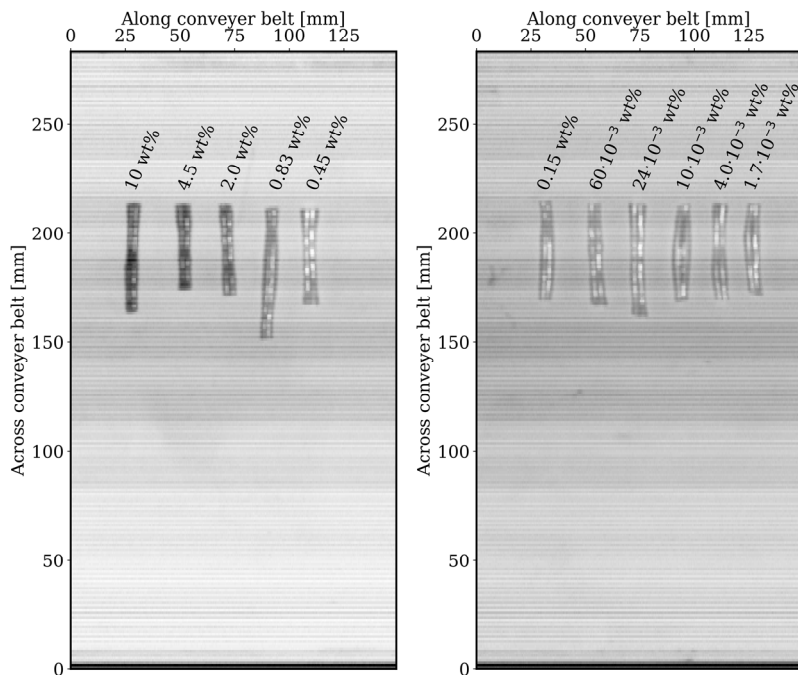
## S4. Hyperspectral camera spectra of all components

Combined, individual and detailed spectra, extracted from the data cube obtained from the hyperspectral camera, of all the samples in the study.

Images of the hyperspectral samples at 504 nm (Vis/NIR).



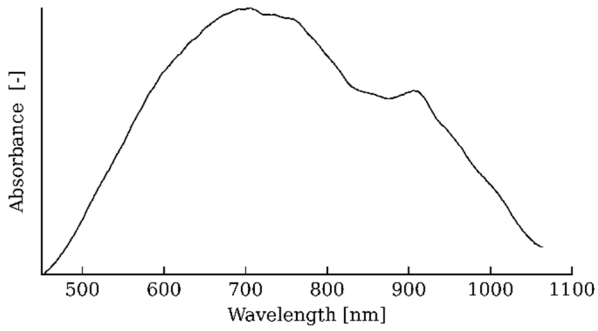
Images of the hyperspectral samples at 1129 nm (SWIR).



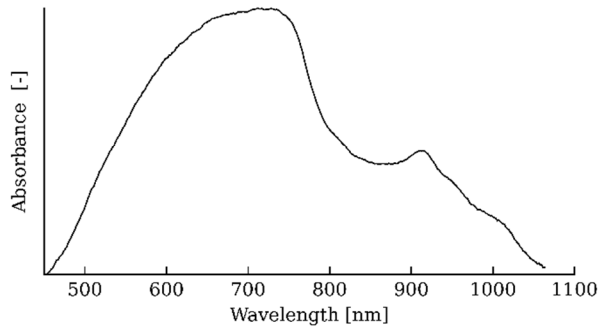
## Individual Vis/NIR Spectra

Individual accumulated spectra of the Vis spectral range extracted from the hyper cube.

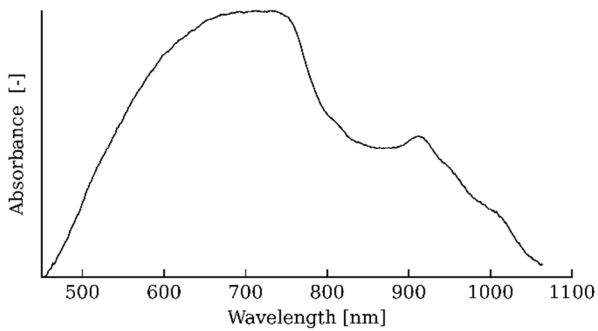
MB 40 wt%



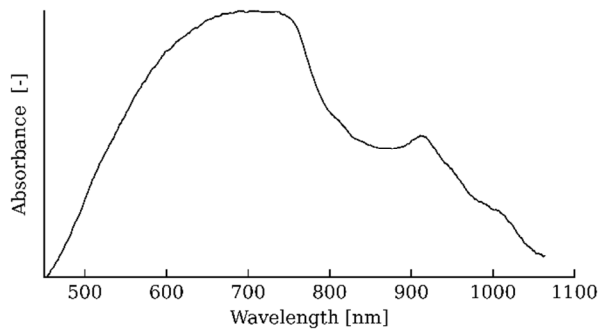
10 wt%



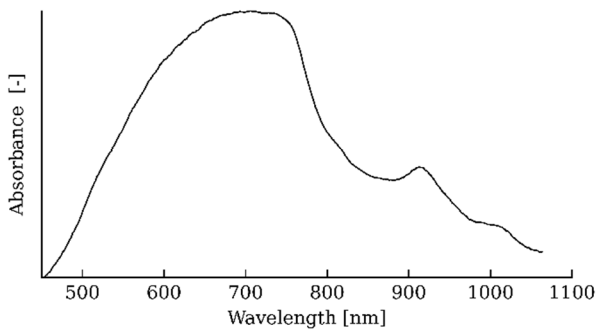
4.5 wt%



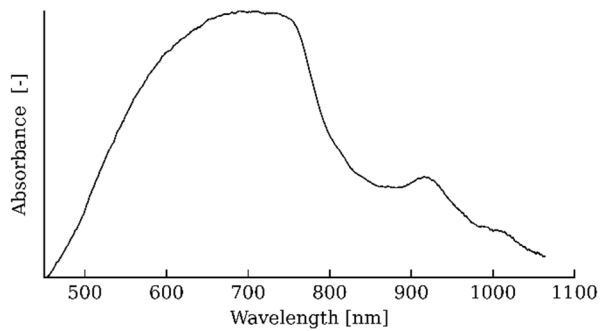
2.0 wt%



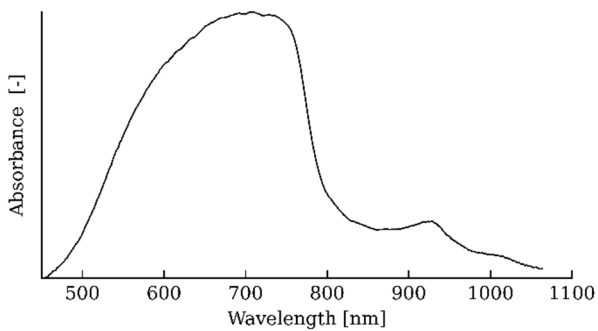
0.83 wt%



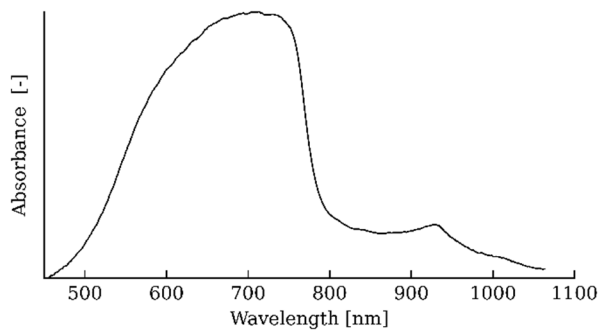
0.35 wt%



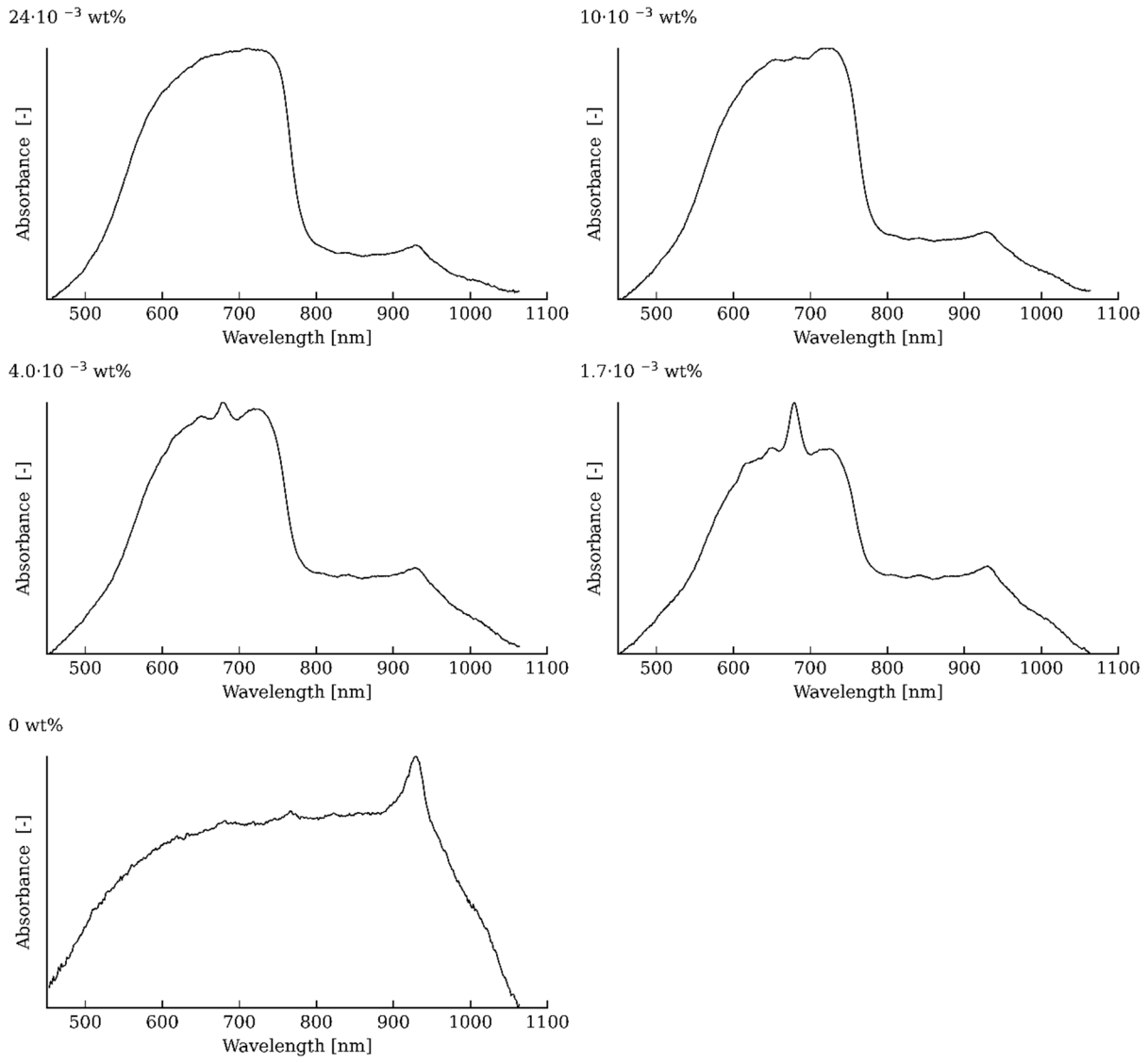
0.15 wt%



$60 \cdot 10^{-3}$  wt%

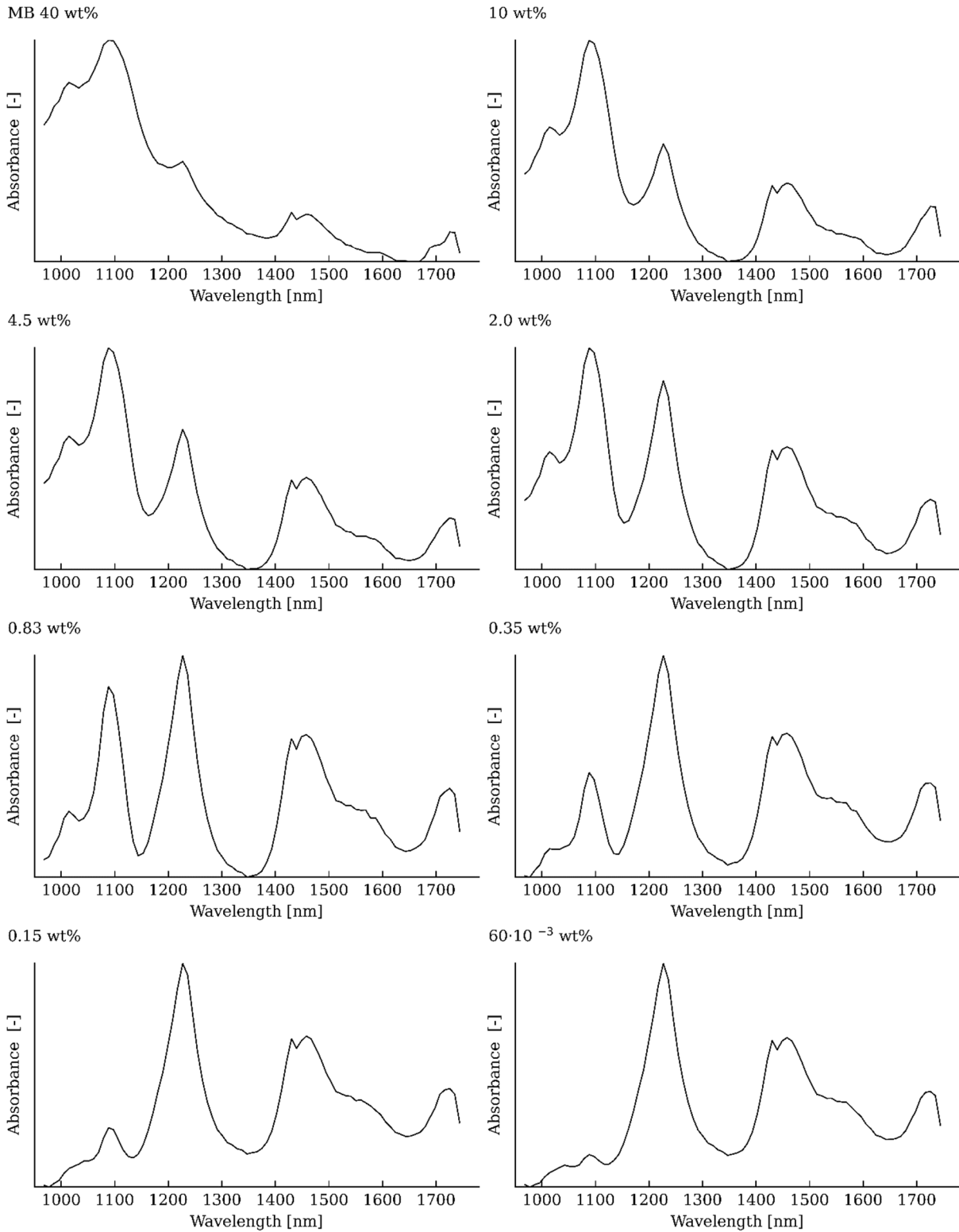


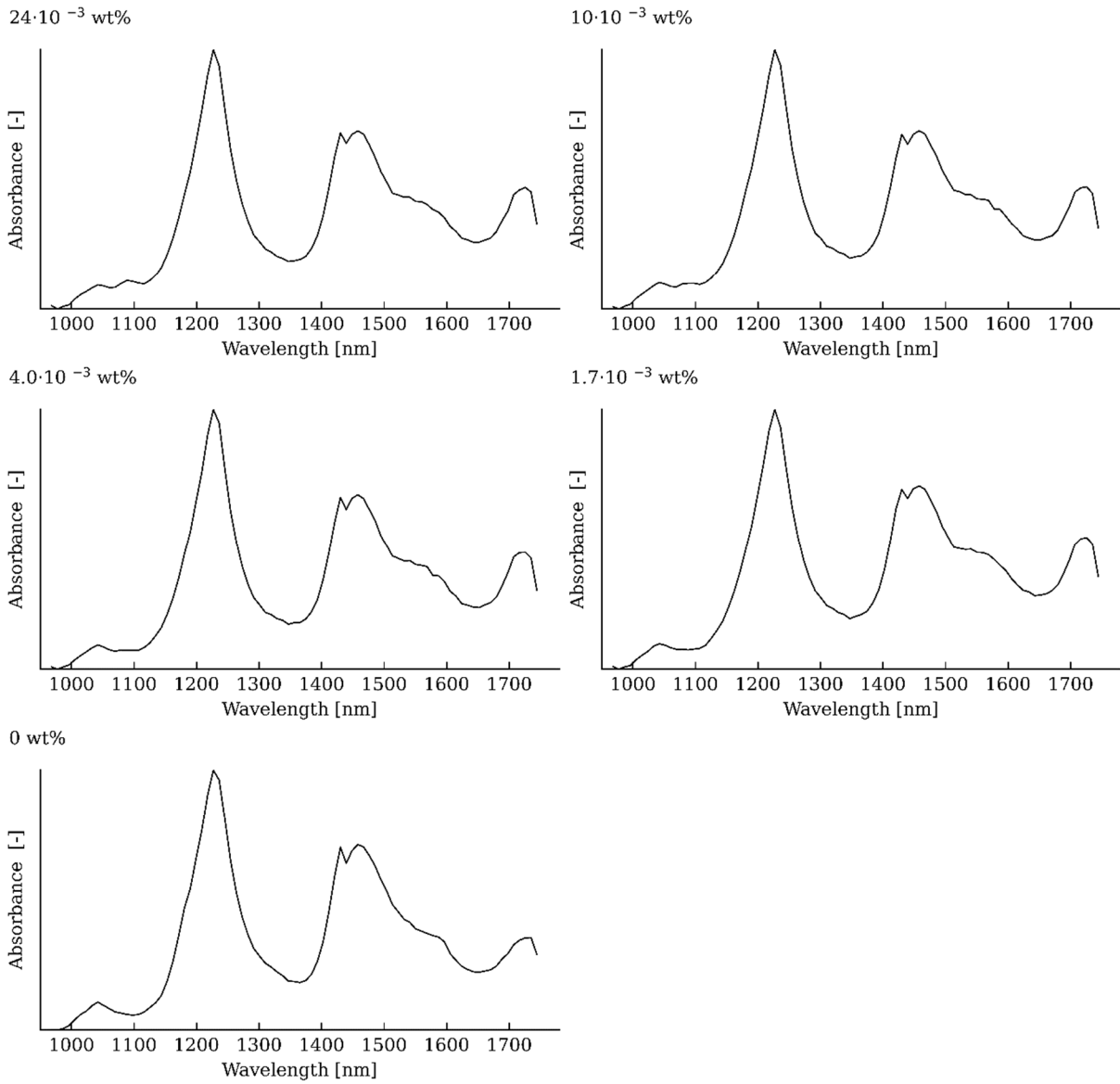




### Individual SWIR spectra

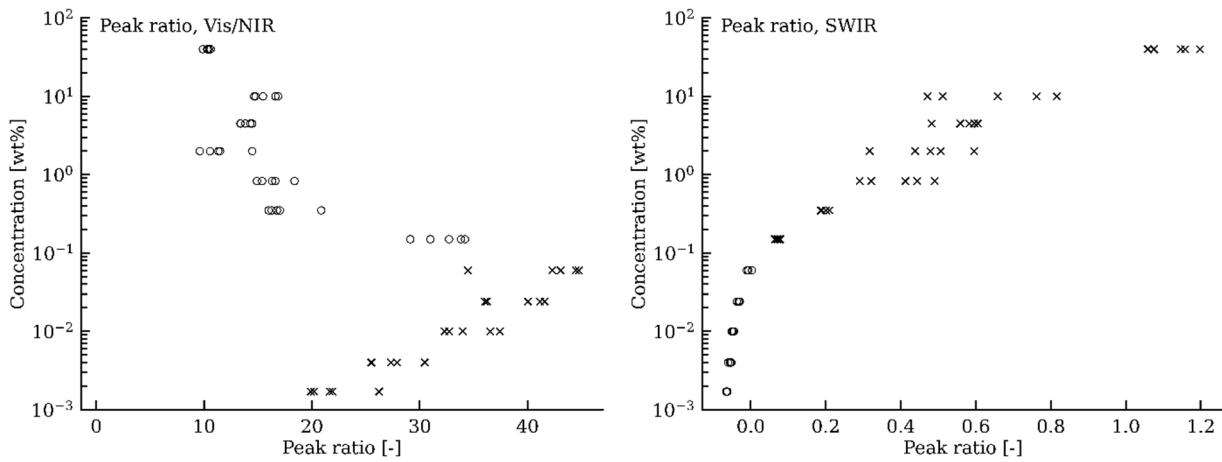
Individual accumulated and normalized spectra of the SWIR spectral range extracted from the hyper cube.





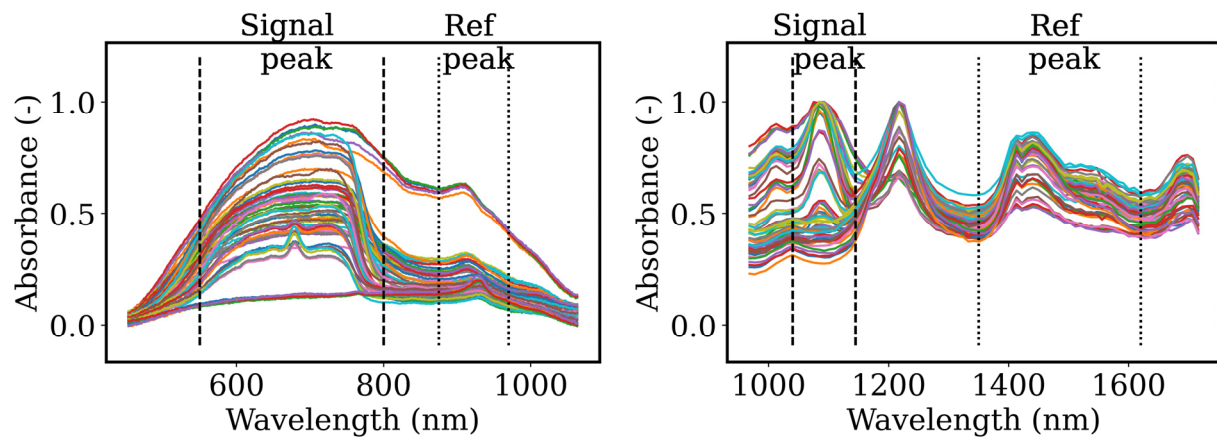
## S5. Peak ratio analysis and concentration modelling

### Detection limit Vis/NIR and SWIR



Symbol times = included and circle = not included.

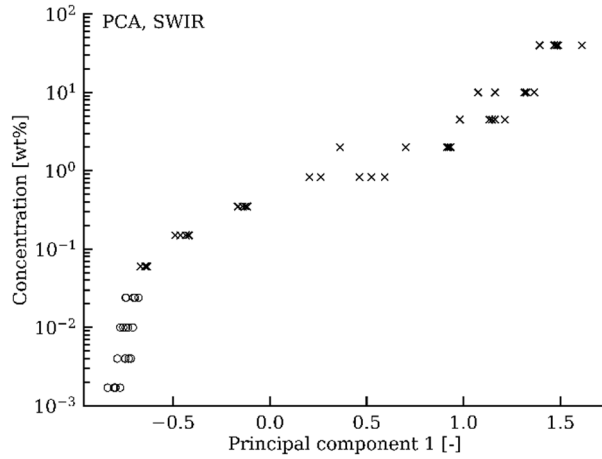
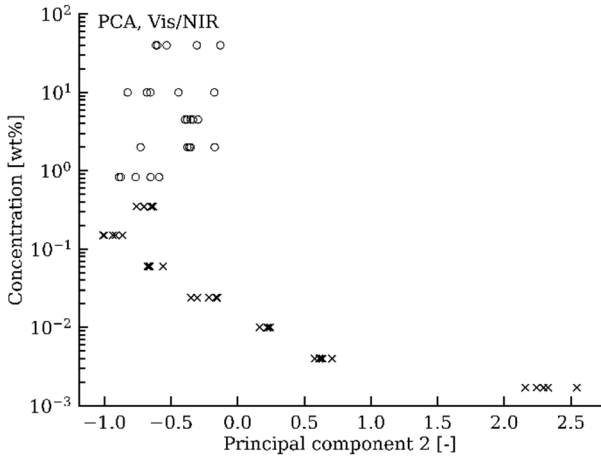
### Integration limit Vis/NIR and SWIR



All the individual spectra can be seen in section S4.

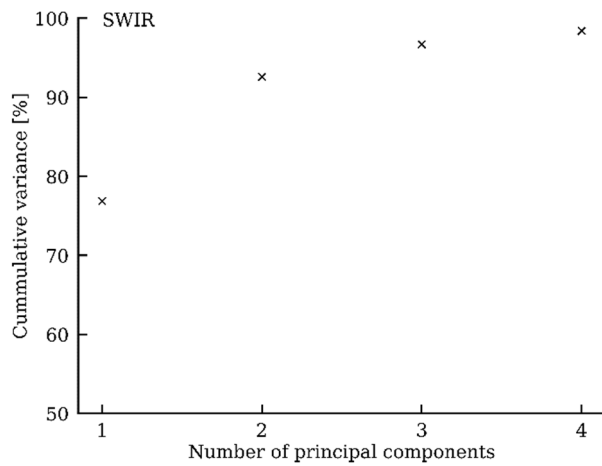
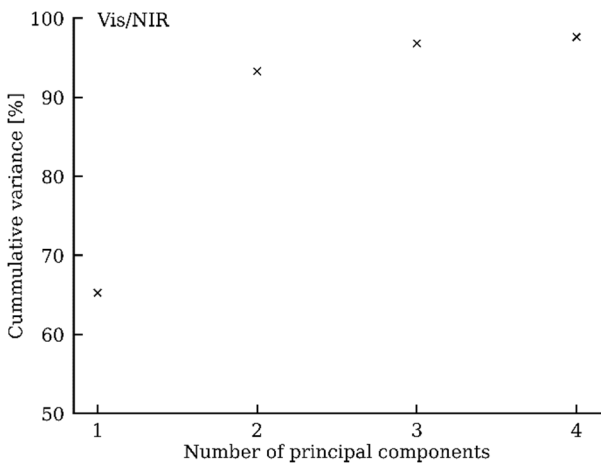
## S6. PCA analysis and concentration modelling

### Detection limit Vis/NIR and SWIR



Symbol times = included and circle = not included.

### Scree plot on optimized Vis/NIR and SWIR



### Loading plots on optimized Vis-NIR and SWIR

